

Anhang A

TABELLE ALLGEMEINER EIGENSCHAFTEN VON LAPLACE-TRANSFORMATIONEN

$$f(s) = \int_0^{\infty} e^{-st} F(t) dt$$

| | $f(s)$ | $F(t)$ |
|------------|--|---|
| 1. | $a f_1(s) + b f_2(s)$ | $a F_1(t) + b F_2(t)$ |
| 2. | $f(s/a)$ | $a F(at)$ |
| 3. | $f(s - a)$ | $e^{at} F(t)$ |
| 4. | $e^{-as} f(s)$ | $u(t-a) = \begin{cases} F(t-a) & t > a \\ 0 & t < a \end{cases}$ |
| 5. | $s f(s) - F(0)$ | $F'(t)$ |
| 6. | $s^2 f(s) - s F(0) - F'(0)$ | $F''(t)$ |
| 7. | $s^n f(s) - s^{n-1} F(0) - s^{n-2} F'(0) - \dots - F^{(n-1)}(0)$ | $F^{(n)}(t)$ |
| 8. | $f'(s)$ | $-t F(t)$ |
| 9. | $f''(s)$ | $t^2 F(t)$ |
| 10. | $f^{(n)}(s)$ | $(-1)^n t^n F(t)$ |
| 11. | $\frac{f(s)}{s}$ | $\int_0^t F(u) du$ |
| 12. | $\frac{f(s)}{s^n}$ | $\int_0^t \dots \int_0^t F(u) du^n = \int_0^t \frac{(t-u)^{n-1}}{(n-1)!} F(u) du$ |
| 13. | $f(s) g(s)$ | $\int_0^t F(u) G(t-u) du$ |

ANHANG A

TABELLE ALLGEMEINER EIGENSCHAFTEN VON LAPLACE-TRANSFORMATIONEN

| | $f(s)$ | $F(t)$ |
|-----|--|--|
| 14. | $\int_s^\infty f(u) du$ | $\frac{F(t)}{t}$ |
| 15. | $\frac{1}{1 - e^{-sT}} \int_0^T e^{-su} F(u) du$ | $F(t) = F(t + T)$ |
| 16. | $\frac{f(\sqrt{s})}{s}$ | $\frac{1}{\sqrt{\pi t}} \int_0^\infty e^{-u^2/4t} F(u) du$ |
| 17. | $\frac{1}{s} f(1/s)$ | $\int_0^\infty J_0(2\sqrt{ut}) F(u) du$ |
| 18. | $\frac{1}{s^{n+1}} f(1/s)$ | $t^{n/2} \int_0^\infty u^{-n/2} J_n(2\sqrt{ut}) F(u) du$ |
| 19. | $\frac{f(s + 1/s)}{s^2 + 1}$ | $\int_0^t J_0(2\sqrt{u(t-u)}) F(u) du$ |
| 20. | $\frac{1}{2\sqrt{\pi}} \int_0^\infty u^{-3/2} e^{-s^2/4u} f(u) du$ | $F(t^2)$ |
| 21. | $\frac{f(\ln s)}{s \ln s}$ | $\int_0^\infty \frac{t^u F(u)}{\Gamma(u+1)} du$ |
| 22. | $\frac{P(s)}{Q(s)}$ $P(s) = \text{Polynom vom Grad kleiner } n,$ $Q(s) = (s - \alpha_1)(s - \alpha_2) \cdots (s - \alpha_n),$ wobei $\alpha_1, \alpha_2, \dots, \alpha_n$ verschieden sind. | $\sum_{k=1}^n \frac{P(\alpha_k)}{Q'(\alpha_k)} e^{\alpha_k t}$ |

Anhang B

TABELLE SPEZIELLER LAPLACE-TRANSFORMATIONEN

| | $f(s)$ | $F(t)$ |
|-----|--|---|
| 1. | $\frac{1}{s}$ | 1 |
| 2. | $\frac{1}{s^2}$ | t |
| 3. | $\frac{1}{s^n} \quad n = 1, 2,$ | $\frac{t^{n-1}}{(n-1)!}, \quad 0! = 1$ |
| 4. | $\frac{1}{s^n} \quad n > 0$ | $\frac{t^{n-1}}{\Gamma(n)}$ |
| 5. | $\frac{1}{s-a}$ | e^{at} |
| 6. | $\frac{1}{(s-a)^n} \quad n = 1, 2, 3, \dots$ | $\frac{t^{n-1} e^{at}}{(n-1)!}, \quad 0! = 1$ |
| 7. | $\frac{1}{(s-a)^n} \quad n > 0$ | $\frac{t^{n-1} e^{at}}{\Gamma(n)}$ |
| 8. | $\frac{1}{s^2 + a^2}$ | $\frac{\sin at}{a}$ |
| 9. | $\frac{s}{s^2 + a^2}$ | $\cos at$ |
| 10. | $\frac{1}{(s-b)^2 + a^2}$ | $\frac{e^{bt} \sin at}{a}$ |
| 11. | $\frac{s-b}{(s-b)^2 + a^2}$ | $e^{bt} \cos at$ |
| 12. | $\frac{1}{s^2 - a^2}$ | $\frac{\sinh at}{a}$ |
| 13. | $\frac{s}{s^2 - a^2}$ | $\cosh at$ |
| 14. | $\frac{1}{(s-b)^2 - a^2}$ | $\frac{e^{bt} \sinh at}{a}$ |

TABELLE SPEZIELLER LAPLACE-TRANSFORMATIONEN

| | $f(s)$ | $F(t)$ |
|-----|---|---|
| 15. | $\frac{s - b}{(s - b)^2 - a^2}$ | $e^{bt} \cosh at$ |
| 16. | $\frac{1}{(s - a)(s - b)} \quad a \neq b$ | $\frac{e^{bt} - e^{at}}{b - a}$ |
| 17. | $\frac{s}{(s - a)(s - b)} \quad a \neq b$ | $\frac{be^{bt} - ae^{at}}{b - a}$ |
| 18. | $\frac{1}{(s^2 + a^2)^2}$ | $\frac{\sin at - at \cos at}{2a^3}$ |
| 19. | $\frac{s}{(s^2 + a^2)^2}$ | $\frac{t \sin at}{2a}$ |
| 20. | $\frac{s^2}{(s^2 + a^2)^2}$ | $\frac{\sin at + at \cos at}{2a}$ |
| 21. | $\frac{s^3}{(s^2 + a^2)^2}$ | $\cos at - \frac{1}{2}at \sin at$ |
| 22. | $\frac{s^2 - a^2}{(s^2 + a^2)^2}$ | $t \cos at$ |
| 23. | $\frac{1}{(s^2 - a^2)^2}$ | $\frac{at \cosh at - \sinh at}{2a^3}$ |
| 24. | $\frac{s}{(s^2 - a^2)^2}$ | $\frac{t \sinh at}{2a}$ |
| 25. | $\frac{s^2}{(s^2 - a^2)^2}$ | $\frac{\sinh at + at \cosh at}{2a}$ |
| 26. | $\frac{s^3}{(s^2 - a^2)^2}$ | $\cosh at + \frac{1}{2}at \sinh at$ |
| 27. | $\frac{s^2 + a^2}{(s^2 - a^2)^2}$ | $t \cosh at$ |
| 28. | $\frac{1}{(s^2 + a^2)^3}$ | $\frac{(3 - a^2t^2) \sin at - 3at \cos at}{8a^5}$ |
| 29. | $\frac{s}{(s^2 + a^2)^3}$ | $\frac{t \sin at - at^2 \cos at}{8a^3}$ |
| 30. | $\frac{s^2}{(s^2 + a^2)^3}$ | $\frac{(1 + a^2t^2) \sin at - at \cos at}{8a^3}$ |
| 31. | $\frac{s^3}{(s^2 + a^2)^3}$ | $\frac{3t \sin at + at^2 \cos at}{8a}$ |

TABELLE SPEZIELLER LAPLACE-TRANSFORMATIONEN

| | $f(s)$ | $F(t)$ |
|-----|---|--|
| 32. | $\frac{s^4}{(s^2 + a^2)^3}$ | $\frac{(3 - a^2t^2) \sin at + 5at \cos at}{8a}$ |
| 33. | $\frac{s^5}{(s^2 + a^2)^3}$ | $\frac{(8 - a^2t^2) \cos at - 7at \sin at}{8}$ |
| 34. | $\frac{3s^2 - a^2}{(s^2 + a^2)^3}$ | $\frac{t^2 \sin at}{2a}$ |
| 35. | $\frac{s^3 - 3a^2s}{(s^2 + a^2)^3}$ | $\frac{1}{2}t^2 \cos at$ |
| 36. | $\frac{s^4 - 6a^2s^2 + a^4}{(s^2 + a^2)^4}$ | $\frac{1}{6}t^3 \cos at$ |
| 37. | $\frac{s^3 - a^2s}{(s^2 + a^2)^4}$ | $\frac{t^3 \sin at}{24a}$ |
| 38. | $\frac{1}{(s^2 - a^2)^3}$ | $\frac{(3 + a^2t^2) \sinh at - 3at \cosh at}{8a^5}$ |
| 39. | $\frac{s}{(s^2 - a^2)^3}$ | $\frac{at^2 \cosh at - t \sinh at}{8a^3}$ |
| 40. | $\frac{s^2}{(s^2 - a^2)^3}$ | $\frac{at \cosh at + (a^2t^2 - 1) \sinh at}{8a^3}$ |
| 41. | $\frac{s^3}{(s^2 - a^2)^3}$ | $\frac{3t \sinh at + at^2 \cosh at}{8a}$ |
| 42. | $\frac{s^4}{(s^2 - a^2)^3}$ | $\frac{(3 + a^2t^2) \sinh at + 5at \cosh at}{8a}$ |
| 43. | $\frac{s^5}{(s^2 - a^2)^3}$ | $\frac{(8 + a^2t^2) \cosh at + 7at \sinh at}{8}$ |
| 44. | $\frac{3s^2 + a^2}{(s^2 - a^2)^3}$ | $\frac{t^2 \sinh at}{2a}$ |
| 45. | $\frac{s^3 + 3a^2s}{(s^2 - a^2)^3}$ | $\frac{1}{2}t^2 \cosh at$ |
| 46. | $\frac{s^4 + 6a^2s^2 + a^4}{(s^2 - a^2)^4}$ | $\frac{1}{6}t^3 \cosh at$ |
| 47. | $\frac{s^3 + a^2s}{(s^2 - a^2)^4}$ | $\frac{t^3 \sinh at}{24a}$ |
| 48. | $\frac{1}{s^3 + a^3}$ | $\frac{e^{at/2}}{3a^2} \left\{ \sqrt{3} \sin \frac{\sqrt{3} at}{2} - \cos \frac{\sqrt{3} at}{2} + e^{-3at/2} \right\}$ |

TABELLE SPEZIELLER LAPLACE-TRANSFORMATIONEN

| | $f(s)$ | $F(t)$ |
|-----|-------------------------------------|--|
| 49. | $\frac{s}{s^3 + a^3}$ | $\frac{e^{at/2}}{3a} \left\{ \cos \frac{\sqrt{3} at}{2} + \sqrt{3} \sin \frac{\sqrt{3} at}{2} - e^{-3at/2} \right\}$ |
| 50. | $\frac{s^2}{s^3 + a^3}$ | $\frac{1}{3} \left(e^{-at} + 2e^{at/2} \cos \frac{\sqrt{3} at}{2} \right)$ |
| 51. | $\frac{1}{s^3 - a^3}$ | $\frac{e^{-at/2}}{3a^2} \left\{ e^{3at/2} - \cos \frac{\sqrt{3} at}{2} - \sqrt{3} \sin \frac{\sqrt{3} at}{2} \right\}$ |
| 52. | $\frac{s}{s^3 - a^3}$ | $\frac{e^{-at/2}}{3a} \left\{ \sqrt{3} \sin \frac{\sqrt{3} at}{2} - \cos \frac{\sqrt{3} at}{2} + e^{3at/2} \right\}$ |
| 53. | $\frac{s^2}{s^3 - a^3}$ | $\frac{1}{3} \left(e^{at} + 2e^{-at/2} \cos \frac{\sqrt{3} at}{2} \right)$ |
| 54. | $\frac{1}{s^4 + 4a^4}$ | $\frac{1}{4a^3} (\sin at \cosh at - \cos at \sinh at)$ |
| 55. | $\frac{s}{s^4 + 4a^4}$ | $\frac{\sin at \sinh at}{2a^2}$ |
| 56. | $\frac{s^2}{s^4 + 4a^4}$ | $\frac{1}{2a} (\sin at \cosh at + \cos at \sinh at)$ |
| 57. | $\frac{s^3}{s^4 + 4a^4}$ | $\cos at \cosh at$ |
| 58. | $\frac{1}{s^4 - a^4}$ | $\frac{1}{2a^3} (\sinh at - \sin at)$ |
| 59. | $\frac{s}{s^4 - a^4}$ | $\frac{1}{2a^2} (\cosh at - \cos at)$ |
| 60. | $\frac{s^2}{s^4 - a^4}$ | $\frac{1}{2a} (\sinh at + \sin at)$ |
| 61. | $\frac{s^3}{s^4 - a^4}$ | $\frac{1}{2} (\cosh at + \cos at)$ |
| 62. | $\frac{1}{\sqrt{s+a} + \sqrt{s+b}}$ | $\frac{e^{-bt} - e^{-at}}{2(b-a)\sqrt{\pi t^3}}$ |
| 63. | $\frac{1}{s\sqrt{s+a}}$ | $\frac{\operatorname{erf} \sqrt{at}}{\sqrt{a}}$ |
| 64. | $\frac{1}{\sqrt{s(s-a)}}$ | $\frac{e^{at} \operatorname{erf} \sqrt{at}}{\sqrt{a}}$ |
| 65. | $\frac{1}{\sqrt{s-a} + b}$ | $e^{at} \left\{ \frac{1}{\sqrt{\pi t}} - b e^{b^2 t} \operatorname{erfc}(b\sqrt{t}) \right\}$ |

TABELLE SPEZIELLER LAPLACE-TRANSFORMATIONEN

| | $f(s)$ | $F(t)$ |
|-----|--|---|
| 66. | $\frac{1}{\sqrt{s^2 + a^2}}$ | $J_0(at)$ |
| 67. | $\frac{1}{\sqrt{s^2 - a^2}}$ | $I_0(at)$ |
| 68. | $\frac{(\sqrt{s^2 + a^2} - s)^n}{\sqrt{s^2 + a^2}} \quad n > -1$ | $a^n J_n(at)$ |
| 69. | $\frac{(s - \sqrt{s^2 - a^2})^n}{\sqrt{s^2 - a^2}} \quad n > -1$ | $a^n I_n(at)$ |
| 70. | $\frac{e^{b(s - \sqrt{s^2 + a^2})}}{\sqrt{s^2 + a^2}}$ | $J_0(a\sqrt{t(t + 2b)})$ |
| 71. | $\frac{e^{-b\sqrt{s^2 + a^2}}}{\sqrt{s^2 + a^2}}$ | $\begin{cases} J_0(a\sqrt{t^2 - b^2}) & t > b \\ 0 & t < b \end{cases}$ |
| 72. | $\frac{1}{(s^2 + a^2)^{3/2}}$ | $\frac{t J_1(at)}{a}$ |
| 73. | $\frac{s}{(s^2 + a^2)^{3/2}}$ | $t J_0(at)$ |
| 74. | $\frac{s^2}{(s^2 + a^2)^{3/2}}$ | $J_0(at) - at J_1(at)$ |
| 75. | $\frac{1}{(s^2 - a^2)^{3/2}}$ | $\frac{t I_1(at)}{a}$ |
| 76. | $\frac{s}{(s^2 - a^2)^{3/2}}$ | $t I_0(at)$ |
| 77. | $\frac{s^2}{(s^2 - a^2)^{3/2}}$ | $I_0(at) + at I_1(at)$ |
| 78. | $\frac{1}{s(e^s - 1)} = \frac{e^{-s}}{s(1 - e^{-s})}$ Siehe auch 141, Seite 254. | $F(t) = n, \quad n \leq t < n + 1, \quad n = 0, 1, 2, \dots$ |
| 79. | $\frac{1}{s(e^s - r)} = \frac{e^{-s}}{s(1 - re^{-s})}$ | $F(t) = \sum_{k=1}^{[t]} r^k$ wobei $[t]$ = größte ganze Zahl $\leq t$ |
| 80. | $\frac{e^s - 1}{s(e^s - r)} = \frac{1 - e^{-s}}{s(1 - re^{-s})}$ Siehe auch 143, Seite 254. | $F(t) = r^n, \quad n \leq t < n + 1, \quad n = 0, 1, 2, \dots$ |
| 81. | $\frac{e^{-a/s}}{\sqrt{s}}$ | $\frac{\cos 2\sqrt{at}}{\sqrt{\pi t}}$ |

TABELLE SPEZIELLER LAPLACE-TRANSFORMATIONEN

| | $f(s)$ | $F(t)$ |
|-----|---|---|
| 82. | $\frac{e^{-a/s}}{s^{3/2}}$ | $\frac{\sin 2\sqrt{at}}{\sqrt{\pi a}}$ |
| 83. | $\frac{e^{-a/s}}{s^{n+1}} \quad n > -1$ | $\left(\frac{t}{a}\right)^{n/2} J_n(2\sqrt{at})$ |
| 84. | $\frac{e^{-a\sqrt{s}}}{\sqrt{s}}$ | $\frac{e^{-a^2/4t}}{\sqrt{\pi t}}$ |
| 85. | $e^{-a\sqrt{s}}$ | $\frac{a}{2\sqrt{\pi t^3}} e^{-a^2/4t}$ |
| 86. | $\frac{1 - e^{-a\sqrt{s}}}{s}$ | $\text{erf}(a/2\sqrt{t})$ |
| 87. | $\frac{e^{-a\sqrt{s}}}{s}$ | $\text{erfc}(a/2\sqrt{t})$ |
| 88. | $\frac{e^{-a\sqrt{s}}}{\sqrt{s}(\sqrt{s} + b)}$ | $e^{b(bt+a)} \text{erfc}\left(b\sqrt{t} + \frac{a}{2\sqrt{t}}\right)$ |
| 89. | $\frac{e^{-a/\sqrt{s}}}{s^{n+1}} \quad n > -1$ | $\frac{1}{\sqrt{\pi t} a^{2n+1}} \int_0^\infty u^n e^{-u^2/4a^2t} J_{2n}(2\sqrt{u}) du$ |
| 90. | $\ln\left(\frac{s+a}{s+b}\right)$ | $\frac{e^{-bt} - e^{-at}}{t}$ |
| 91. | $\frac{\ln[(s^2 + a^2)/a^2]}{2s}$ | $\text{Ci}(at)$ |
| 92. | $\frac{\ln[(s+a)/a]}{s}$ | $\text{Ei}(at)$ |
| 93. | $-\frac{(\gamma + \ln s)}{s}$ $\gamma = \text{Eulersche Konstante} = 0,5772156\dots$ | $\ln t$ |
| 94. | $\ln\left(\frac{s^2 + a^2}{s^2 + b^2}\right)$ | $\frac{2(\cos at - \cos bt)}{t}$ |
| 95. | $\frac{\pi^2}{6s} + \frac{(\gamma + \ln s)^2}{s}$ $\gamma = \text{Eulersche Konstante} = 0,5772156\dots$ | $\ln^2 t$ |
| 96. | $\frac{\ln s}{s}$ | $-(\ln t + \gamma)$ $\gamma = \text{Eulersche Konstante} = 0,5772156\dots$ |
| 97. | $\frac{\ln^2 s}{s}$ | $(\ln t + \gamma)^2 - \frac{1}{6}\pi^2$ $\gamma = \text{Eulersche Konstante} = 0,5772156\dots$ |

TABELLE SPEZIELLER LAPLACE-TRANSFORMATIONEN

| | $f(s)$ | $F(t)$ |
|------|---|--|
| 98. | $\frac{\Gamma'(n+1) - \Gamma'(n+1) \ln s}{s^{n+1}} \quad n > -1$ | $t^n \ln t$ |
| 99. | $\tan^{-1}(a/s)$ | $\frac{\sin at}{t}$ |
| 100. | $\frac{\tan^{-1}(a/s)}{s}$ | $\text{Si}(at)$ |
| 101. | $\frac{e^{a/s}}{\sqrt{s}} \text{erfc}(\sqrt{a/s})$ | $\frac{e^{-2\sqrt{at}}}{\sqrt{\pi t}}$ |
| 102. | $e^{s^2/4a^2} \text{erfc}(s/2a)$ | $\frac{2a}{\sqrt{\pi}} e^{-a^2 t^2}$ |
| 103. | $\frac{e^{s^2/4a^2} \text{erfc}(s/2a)}{s}$ | $\text{erf}(at)$ |
| 104. | $\frac{e^{as} \text{erfc} \sqrt{as}}{\sqrt{s}}$ | $\frac{1}{\sqrt{\pi(t+a)}}$ |
| 105. | $e^{as} \text{Ei}(as)$ | $\frac{1}{t+a}$ |
| 106. | $\frac{1}{a} \left[\cos as \left\{ \frac{\pi}{2} - \text{Si}(as) \right\} - \sin as \text{Ci}(as) \right]$ | $\frac{1}{t^2 + a^2}$ |
| 107. | $\sin as \left\{ \frac{\pi}{2} - \text{Si}(as) \right\} + \cos as \text{Ci}(as)$ | $\frac{t}{t^2 + a^2}$ |
| 108. | $\frac{\cos as \left\{ \frac{\pi}{2} - \text{Si}(as) \right\} - \sin as \text{Ci}(as)}{s}$ | $\tan^{-1}(t/a)$ |
| 109. | $\frac{\sin as \left\{ \frac{\pi}{2} - \text{Si}(as) \right\} + \cos as \text{Ci}(as)}{s}$ | $\frac{1}{2} \ln \left(\frac{t^2 + a^2}{a^2} \right)$ |
| 110. | $\left[\frac{\pi}{2} - \text{Si}(as) \right]^2 + \text{Ci}^2(as)$ | $\frac{1}{t} \ln \left(\frac{t^2 + a^2}{a^2} \right)$ |
| 111. | 0 | $\mathcal{N}(t)$ |
| 112. | 1 | $\delta(t)$ |
| 113. | e^{-as} | $\delta(t-a)$ |
| 114. | $\frac{e^{-as}}{s}$ Siehe auch 139, Seite 254. | $u(t-a)$ |

TABELLE SPEZIELLER LAPLACE-TRANSFORMATIONEN

| | $f(s)$ | $F(t)$ |
|------|--|--|
| 115. | $\frac{\sinh sx}{s \sinh sa}$ | $\frac{x}{a} + \frac{2}{\pi} \sum_{n=1}^{\infty} \frac{(-1)^n}{n} \sin \frac{n\pi x}{a} \cos \frac{n\pi t}{a}$ |
| 116. | $\frac{\sinh sx}{s \cosh sa}$ | $\frac{4}{\pi} \sum_{n=1}^{\infty} \frac{(-1)^n}{2n-1} \sin \frac{(2n-1)\pi x}{2a} \sin \frac{(2n-1)\pi t}{2a}$ |
| 117. | $\frac{\cosh sx}{s \sinh sa}$ | $\frac{t}{a} + \frac{2}{\pi} \sum_{n=1}^{\infty} \frac{(-1)^n}{n} \cos \frac{n\pi x}{a} \sin \frac{n\pi t}{a}$ |
| 118. | $\frac{\cosh sx}{s \cosh sa}$ | $1 + \frac{4}{\pi} \sum_{n=1}^{\infty} \frac{(-1)^n}{2n-1} \cos \frac{(2n-1)\pi x}{2a} \cos \frac{(2n-1)\pi t}{2a}$ |
| 119. | $\frac{\sinh sx}{s^2 \sinh sa}$ | $\frac{xt}{a} + \frac{2a}{\pi^2} \sum_{n=1}^{\infty} \frac{(-1)^n}{n^2} \sin \frac{n\pi x}{a} \sin \frac{n\pi t}{a}$ |
| 120. | $\frac{\sinh sx}{s^2 \cosh sa}$ | $x + \frac{8a}{\pi^2} \sum_{n=1}^{\infty} \frac{(-1)^n}{(2n-1)^2} \sin \frac{(2n-1)\pi x}{2a} \cos \frac{(2n-1)\pi t}{2a}$ |
| 121. | $\frac{\cosh sx}{s^2 \sinh sa}$ | $\frac{t^2}{2a} + \frac{2a}{\pi^2} \sum_{n=1}^{\infty} \frac{(-1)^n}{n^2} \cos \frac{n\pi x}{a} \left(1 - \cos \frac{n\pi t}{a}\right)$ |
| 122. | $\frac{\cosh sx}{s^2 \cosh sa}$ | $t + \frac{8a}{\pi^2} \sum_{n=1}^{\infty} \frac{(-1)^n}{(2n-1)^2} \cos \frac{(2n-1)\pi x}{2a} \sin \frac{(2n-1)\pi t}{2a}$ |
| 123. | $\frac{\cosh sx}{s^3 \cosh sa}$ | $\frac{1}{2}(t^2 + x^2 - a^2) - \frac{16a^2}{\pi^3} \sum_{n=1}^{\infty} \frac{(-1)^n}{(2n-1)^3} \cos \frac{(2n-1)\pi x}{2a} \cos \frac{(2n-1)\pi t}{2a}$ |
| 124. | $\frac{\sinh x\sqrt{s}}{\sinh a\sqrt{s}}$ | $\frac{2\pi}{a^2} \sum_{n=1}^{\infty} (-1)^n n e^{-n^2\pi^2 t/a^2} \sin \frac{n\pi x}{a}$ |
| 125. | $\frac{\cosh x\sqrt{s}}{\cosh a\sqrt{s}}$ | $\frac{\pi}{a^2} \sum_{n=1}^{\infty} (-1)^{n-1} (2n-1) e^{-(2n-1)^2\pi^2 t/4a^2} \cos \frac{(2n-1)\pi x}{2a}$ |
| 126. | $\frac{\sinh x\sqrt{s}}{\sqrt{s} \cosh a\sqrt{s}}$ | $\frac{2}{a} \sum_{n=1}^{\infty} (-1)^{n-1} e^{-(2n-1)^2\pi^2 t/4a^2} \sin \frac{(2n-1)\pi x}{2a}$ |
| 127. | $\frac{\cosh x\sqrt{s}}{\sqrt{s} \sinh a\sqrt{s}}$ | $\frac{1}{a} + \frac{2}{a} \sum_{n=1}^{\infty} (-1)^n e^{-n^2\pi^2 t/a^2} \cos \frac{n\pi x}{a}$ |
| 128. | $\frac{\sinh x\sqrt{s}}{s \sinh a\sqrt{s}}$ | $\frac{x}{a} + \frac{2}{\pi} \sum_{n=1}^{\infty} \frac{(-1)^n}{n} e^{-n^2\pi^2 t/a^2} \sin \frac{n\pi x}{a}$ |
| 129. | $\frac{\cosh x\sqrt{s}}{s \cosh a\sqrt{s}}$ | $1 + \frac{4}{\pi} \sum_{n=1}^{\infty} \frac{(-1)^n}{2n-1} e^{-(2n-1)^2\pi^2 t/4a^2} \cos \frac{(2n-1)\pi x}{2a}$ |
| 130. | $\frac{\sinh x\sqrt{s}}{s^2 \sinh a\sqrt{s}}$ | $\frac{xt}{a} + \frac{2a^2}{\pi^3} \sum_{n=1}^{\infty} \frac{(-1)^n}{n^3} (1 - e^{-n^2\pi^2 t/a^2}) \sin \frac{n\pi x}{a}$ |
| 131. | $\frac{\cosh x\sqrt{s}}{s^2 \cosh a\sqrt{s}}$ | $\frac{1}{2}(x^2 - a^2) + t - \frac{16a^2}{\pi^3} \sum_{n=1}^{\infty} \frac{(-1)^n}{(2n-1)^3} e^{-(2n-1)^2\pi^2 t/4a^2} \cos \frac{(2n-1)\pi x}{2a}$ |

TABELLE SPEZIELLER LAPLACE-TRANSFORMATIONEN

| | $f(s)$ | $F(t)$ |
|------|--|---|
| 132. | $\frac{J_0(ix\sqrt{s})}{s J_0(ia\sqrt{s})}$ | $1 - 2 \sum_{n=1}^{\infty} \frac{e^{-\lambda_n^2 t/a^2} J_0(\lambda_n x/a)}{\lambda_n J_1(\lambda_n)}$ wobei $\lambda_1, \lambda_2, \dots$ die positiven Wurzeln von $J_0(\lambda) = 0$ sind |
| 133. | $\frac{J_0(ix\sqrt{s})}{s^2 J_0(ia\sqrt{s})}$ | $\frac{1}{4}(x^2 - a^2) + t + 2a^2 \sum_{n=1}^{\infty} \frac{e^{-\lambda_n^2 t/a^2} J_0(\lambda_n x/a)}{\lambda_n^3 J_1(\lambda_n)}$ wobei $\lambda_1, \lambda_2, \dots$ die positiven Wurzeln von $J_0(\lambda) = 0$ sind |
| 134. | $\frac{1}{as^2} \tanh\left(\frac{as}{2}\right)$ | |
| 135. | $\frac{1}{s} \tanh\left(\frac{as}{2}\right)$ | |
| 136. | $\frac{\pi a}{a^2 s^2 + \pi^2} \coth\left(\frac{as}{2}\right)$ | Rektifizierte Sinuskurve |
| 137. | $\frac{\pi a}{(a^2 s^2 + \pi^2)(1 - e^{-as})}$ | Abgeschnittene Sinuskurve |
| 138. | $\frac{1}{as^2} - \frac{e^{-as}}{s(1 - e^{-as})}$ | Sägezahnfunktion |

TABELLE SPEZIELLER LAPLACE-TRANSFORMATIONEN

| | $f(s)$ | $F(t)$ |
|------|--|---|
| 139. | $\frac{e^{-as}}{s}$ Siehe auch 114, Seite 251. | Heavisidesche Sprungfunktion $u(t-a)$ |
| 140. | $\frac{e^{-as}(1 - e^{-\epsilon s})}{s}$ | |
| 141. | $\frac{1}{s(1 - e^{-as})}$ Siehe auch 78, Seite 249. | Treppenfunktion |
| 142. | $\frac{e^{-s} + e^{-2s}}{s(1 - e^{-s})^2}$ | $F(t) = n^2, \quad n \leq t < n+1, \quad n = 0, 1, 2, \dots$ |
| 143. | $\frac{1 - e^{-s}}{s(1 - re^{-s})}$ Siehe auch 80, Seite 249. | $F(t) = r^n, \quad n \leq t < n+1, \quad n = 0, 1, 2, \dots$ |
| 144. | $\frac{\pi a(1 + e^{-as})}{a^2 s^2 + \pi^2}$ | $F(t) = \begin{cases} \sin(\pi t/a) & 0 \leq t \leq a \\ 0 & t > a \end{cases}$ |